

# High-resolution luminescence spectroscopy study of down-conversion routes in $\text{NaGdF}_4:\text{Nd}^{3+}$ and $\text{NaGdF}_4:\text{Tm}^{3+}$ using synchrotron radiation

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(Received 2 August 2007; published 10 March 2008)

Down-conversion in lanthanide doped luminescent materials is a promising route to significantly enhance the energy efficiency of silicon solar cells, plasma display panels, or mercury-free lighting tubes because it results in the emission of two photons for each absorbed higher energy photon. The  $\text{Gd}^{3+}/\text{Eu}^{3+}$  ion couple shows down-conversion of vacuum-ultraviolet light into visible light with an efficiency close to 190%. The low absorption strength of the  ${}^6G_{7/2}$  levels of  $\text{Gd}^{3+}$  (the starting point of the down-conversion process), however, prevents efficient excitation of the down-conversion process and therefore application. We have performed a high resolution luminescence spectroscopy study, using synchrotron radiation, in order to investigate the possibility to use the strong  $4f \rightarrow 5d$  absorption transitions of  $\text{Nd}^{3+}$  and  $\text{Tm}^{3+}$  to sensitize the high energy  ${}^6G_{7/2}$  level of  $\text{Gd}^{3+}$  in the phosphors  $\text{NaGdF}_4:2\%\text{Nd}^{3+}$  and  $\text{NaGdF}_4:2\%\text{Tm}^{3+}$ .  $\text{Tm}^{3+}$  appears to be an efficient sensitizer of the  ${}^6G_{7/2}$  state of  $\text{Gd}^{3+}$ . It was also found that sensitization is followed by two successive energy transfer processes exciting two  $\text{Tm}^{3+}$  ions in the  ${}^3H_4$  state which results in the emission of two infrared photons for one absorbed vacuum-ultraviolet photon.  $\text{Nd}^{3+}$  is not a good sensitizer of the  ${}^6G_{7/2}$  state in  $\text{NaGdF}_4$ . Instead  $\text{Nd}^{3+}$  efficiently transfers its energy by cross relaxation to the lower energy  ${}^6D_J$  states of  $\text{Gd}^{3+}$  but leaving the  $\text{Nd}^{3+}$  ion excited in the  ${}^4F_{3/2}$  state. Successive energy transfer from  $\text{Gd}^{3+}$  back to  $\text{Nd}^{3+}$  excites a second  $\text{Nd}^{3+}$  ion in the  ${}^4F_{3/2}$  state. Also, in this case, two infrared photons can be emitted for one absorbed vacuum-ultraviolet photon.

DOI: 10.1103/PhysRevB.77.125110

PACS number(s): 78.40.Ha, 71.70.Gm, 78.47.-p, 78.55.Hx

## I. INTRODUCTION

There is a real need for luminescent materials that emit two visible or infrared (IR) photons for each absorbed vacuum-ultraviolet (VUV) or ultraviolet (UV) photon. Such quantum cutting (or quantum splitting) phosphors can be applied in plasma display panels (PDPs), Hg-free lighting tubes, or solar cells to raise energy efficiency.<sup>1-4</sup>

In PDPs and Hg-free lighting, phosphors are applied, which need to convert high energy VUV light from a noble gas discharge (between 7 and 9 eV) into visible red, green, and blue lights (1.7–3 eV).<sup>5</sup> Although the quantum efficiency of currently applied conventional phosphors is close to the possible maximum (100%),<sup>6</sup> the energy efficiency is rather low due to the large difference between the excitation and emission energies. Application of quantum cutting phosphors can, in principle, raise the energy efficiency by a factor of 2.<sup>1</sup>

Silicon solar cells hamper with a very similar problem. Although the UV and visible part of the solar spectrum is efficiently absorbed by silicon, the excitation energy in excess of the silicon band gap that is about 1.2 eV is lost by thermalization. It has been calculated that in the ideal case, a quantum cutting luminescent material converting UV and visible light into IR light can enhance the energy efficiency of a solar cell from 29% to 37%.<sup>4</sup>

The phenomena of quantum cutting can be achieved by an energy relaxation mechanisms generally referred to as down-conversion. Wegh *et al.*<sup>1</sup> discovered a promising phosphor  $\text{LiGdF}_4:\text{Eu}^{3+}$ , in which down-conversion is achieved by a

two step energy transfer process between two different lanthanide ions  $\text{Gd}^{3+}$  and  $\text{Eu}^{3+}$  (see Fig. 1). After a  $\text{Gd}^{3+}$  ion has been excited into the high energy  ${}^6G_{7/2}$  state, cross relaxation occurs between  $\text{Gd}^{3+}$  and  $\text{Eu}^{3+}$  (dashed arrows) resulting in an excited  $\text{Eu}^{3+}$  ion ready to emit a red photon. Cross relaxation is followed by a second energy transfer step from  $\text{Gd}^{3+}$  (curved arrow) that excites a second  $\text{Eu}^{3+}$  ion that will emit a

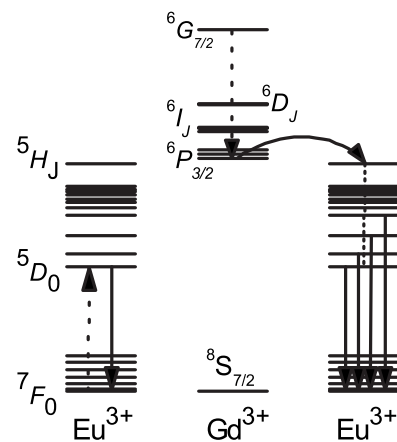


FIG. 1. Schematic energy level diagram of  $\text{Gd}^{3+}$  and  $\text{Eu}^{3+}$  in  $\text{LiGdF}_4$ . The observed quantum splitting process by down-conversion involving cross relaxation (dashed arrows), energy transfer (curved arrow), and multiphonon relaxation (dotted arrow) leads to the emission of two red photons by  $\text{Eu}^{3+}$  (solid arrows) for each  $\text{Gd}^{3+}$  ion that is excited in its  ${}^6G_{7/2}$  state. Note that for clarity, not all energy levels are shown.

second red photon. The quantum efficiency of  $\text{LiGdF}_4:\text{Eu}^{3+}$  was reported to be close to 190%.<sup>1</sup>

A drawback of this phosphor is the low absorption efficiency into the high energy  ${}^6G_{7/2}$  state of  $\text{Gd}^{3+}$ . The absorption transition is spin and parity forbidden and, therefore, weak. These problems were emphasized by Feldmann *et al.*<sup>7</sup> who showed that the external quantum efficiency, a more practical quantity that also takes into account the absorption efficiency of  $\text{LiGdF}_4:\text{Eu}^{3+}$ , was only 32%. Clearly, the sensitization of high energy  ${}^6G_{7/2}$  state of  $\text{Gd}^{3+}$  is of crucial importance.

Several reports can be found in literature on the sensitization of  $\text{Gd}^{3+}$  by other ions with high absorption cross section and efficient energy transfers to the  ${}^6G_{7/2}$  state of  $\text{Gd}^{3+}$ . Babin *et al.*<sup>8</sup> considered the role of  $\text{Pb}^{2+}$  as a sensitizer for the  ${}^6G_{7/2}$  state of  $\text{Gd}^{3+}$ . Peijzel *et al.*<sup>9</sup> successfully used  $\text{Tm}^{3+}$  as a sensitizer in  $\text{LiGdF}_4:\text{Eu}^{3+}, \text{Tm}^{3+}$  but discovered at the same time that the cross-relaxation step from  $\text{Gd}^{3+}$  to  $\text{Eu}^{3+}$ , described above Fig. 1, was quenched by more efficient cross relaxation from  $\text{Gd}^{3+}$  to  $\text{Tm}^{3+}$ . A similar competing cross relaxation from  $\text{Gd}^{3+}$  to  $\text{Nd}^{3+}$  was found by Jia *et al.* in  $\text{LiGdF}_4:\text{Nd}^{3+}$ .<sup>10</sup>

In this work, the ions  $\text{Nd}^{3+}$  and  $\text{Tm}^{3+}$  in hexagonal  $\text{NaGdF}_4$  are investigated as potential sensitizers for the high energy  $\text{Gd}^{3+} {}^6G_{7/2}$  state. In  $\text{NaGdF}_4$ , both ions have  $5d$  states at higher energies than the  $\text{Gd}^{3+} {}^6G_{7/2}$  state which makes energy transfer energetically possible. They also have no  $4f$  levels close in energy below the  $5d$  states, which makes a nonradiative relaxation from the  $5d$  states to the  $4f$  states of  $\text{Tm}^{3+}$  or  $\text{Nd}^{3+}$  improbable. In addition, these ions are expected to have  $5d \rightarrow 4f$  emission bands that spectrally overlap with the  $\text{Gd}^{3+} {}^6G_j$  states, which makes a resonant energy transfer from  $\text{Nd}^{3+}$  or  $\text{Tm}^{3+}$  to  $\text{Gd}^{3+}$  possible.

The host material  $\text{NaGdF}_4$  is a member of the hexagonal  $\text{NaNF}_4$  family ( $\text{Ln}=\text{Y}, \text{La-Lu}$ ). Its structure was first determined for  $\text{NaNdF}_4$ ,<sup>11</sup> and its  $\text{Na}^+/\text{Ln}^{3+}$  disorder was recently refined for  $\text{NaLaF}_4$  and  $\text{NaGdF}_4$ .<sup>12</sup> Due to its cation disorder, the two slightly different  $\text{Ln}^{3+}$  sites and the short Ln-Ln distances of two times 3.61 Å and six times 3.92 Å for the example of  $\text{NaGdF}_4$ , it is the most efficient up-conversion host lattice<sup>13</sup> hitherto known. Thus, strong Ln-Ln interactions are expected for  $\text{NaGdF}_4:\text{Nd}^{3+}$  and  $\text{Tm}^{3+}$  compounds, too.

This paper is organized as follows. First, experimental results on single doped  $\text{NaLaF}_4:2\% \text{Nd}^{3+}$  are presented to establish the dominant emission characteristics of  $\text{Nd}^{3+}$  in this host. Second, the energy transfer mechanisms from  $\text{Nd}^{3+}$  to  $\text{Gd}^{3+}$  are investigated in hexagonal  $\text{NaGdF}_4:\text{Nd}^{3+}$ , and conclusions are drawn about the sensitizing potential of  $\text{Nd}^{3+}$ . Third, the focus will be on a possible energy back transfer from  $\text{Gd}^{3+}$  to  $\text{Nd}^{3+}$ . Finally, the same investigations are presented and discussed for  $\text{Tm}^{3+}$  in hexagonal  $\text{NaGdF}_4$ .

## II. EXPERIMENTAL PROCEDURES

### A. Materials synthesis

Powder samples of phase-pure hexagonal  $\text{NaLaF}_4:2\% M^{3+}$  and  $\text{NaGdF}_4:2\% M^{3+}$  ( $M=\text{Nd}$  or  $\text{Tm}$ ) fluorides were prepared from rare-earth oxides  $\text{Re}_2\text{O}_3$  ( $\text{Re}=\text{La},$

$\text{Nd}, \text{Gd},$  and  $\text{Tm}$ ) of 5N or 6N purity (Metal Rare Earth Ltd.),  $\text{Na}_2\text{CO}_3$  (Alfa, 5N), and aqueous 65%  $\text{HNO}_3$  (Merck, p.a.) and 40%  $\text{HF}$  acids (Merck, supra pure). Batches were typically calculated for 5 g of product. The stoichiometric mixture of the respective rare-earth oxides was dissolved in a small amount of  $\text{HNO}_3$  in a Teflon beaker, evaporated to dryness, dissolved in water, and the fluorides  $\text{MF}_3$  precipitated with  $\text{HF}$ . The liquid is evaporated and  $\text{HF}$  is added again. For the work with  $\text{HF}$  acid or gas, appropriate safety precautions have to be taken. The respective amount of  $\text{Na}_2\text{CO}_3$  to obtain a 2:1 ratio of Na to  $M$  is dissolved in water in a separate beaker and slowly added to the mixture. Care has to be taken to avoid spilling due to the  $\text{CO}_2$  evolution. The product is dried, and the addition of  $\text{HF}$  and drying are repeated. The solid, which consists of a mixture of  $\text{MF}_3$  and  $\text{NaF}$  according to x-ray diffraction, is ground up in a mortar, transferred into a glassy carbon boat, and heated to 550 °C in a  $\text{HF}/\text{Ar}$  gas stream for 20 h. The sample is heated in a tubular furnace in a gas tight nickel apparatus (alloy 600) which is inert to  $\text{HF}$  gas. In this step, the reaction toward hexagonal  $\text{NaMF}_4$  plus excess  $\text{NaF}$  takes place. Traces of O are removed by the  $\text{HF}$  gas stream. The powder is ground up again and heated to 590 °C in an Ar gas stream for another 20 h. This step improves the crystallinity and optical properties of the material. Finally, the product is washed with water to dissolve the excess  $\text{NaF}$  and then dried at 100 °C. All samples were checked by x-ray powder diffraction. They show the hexagonal  $\text{NaLaF}_4$  phase<sup>12,13</sup> together with a small residue of about 0.5%  $\text{NaF}$ .

### B. Spectroscopic measurements

Luminescence excitation spectra were recorded at the Deutsche Elektronen-Synchrotron (DESY) in Hamburg (Germany) using the SUPERLUMI station of HASYLAB. The spectral region of excitation was 50–335 nm with a fixed resolution of 0.3 nm. A R6358P Hamamatsu photomultiplier tube (PMT) connected to a triple grating Czerny-Turner monochromator SpectraPro-308i from Acton Research, Inc., was used to measure excitation spectra of UV to visible luminescence. All excitation spectra were corrected for the wavelength dependent excitation intensity. Details of this excitation facility were described elsewhere.<sup>14</sup>

Luminescence emission spectra were recorded with a liquid nitrogen cooled charge coupled device (CCD) detector of Princeton Instruments, Inc., connected to the monochromator described above. The sensitive spectral range was between 200 and 1100 nm with a resolution close to 1 nm. All emission spectra were corrected for the wavelength dependent detection efficiency. Time resolved emission spectra were recorded with a fast PMT connected to the same monochromator by setting a desired time window (gate) after pulsed synchrotron excitation. All presented data were recorded at 10 K.

## III. EXPERIMENTAL RESULTS AND DISCUSSION

### A. Vacuum-ultraviolet spectroscopy of $\text{NaLaF}_4:2\% \text{Nd}^{3+}$

Figure 2 combines the emission spectrum of  $\text{NaLaF}_4:\text{Nd}^{3+}$  under excitation at 156 nm [curve (b)] and the

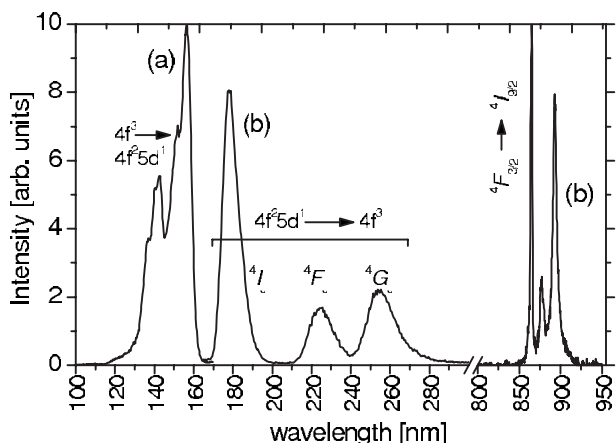


FIG. 2. (a) Excitation spectrum of NaLaF<sub>4</sub>:2%Nd<sup>3+</sup> monitoring the Nd<sup>3+</sup> 4f<sup>2</sup>5d<sup>1</sup> → 4f<sup>3</sup> emission at 178 nm. (b) Emission spectrum of NaLaF<sub>4</sub>:2%Nd<sup>3+</sup> excited in the 4f<sup>2</sup>5d<sup>1</sup> states of Nd<sup>3+</sup> at 156 nm. Both spectra were recorded at 10 K.

excitation spectrum (curve a) monitoring the Nd<sup>3+</sup> emission at 178 nm. The excitation spectrum shows bands between 130 and 160 nm corresponding to the 4f<sup>2</sup>5d<sup>1</sup> configuration of Nd<sup>3+</sup>. The emission spectrum consists of both 4f<sup>2</sup>5d<sup>1</sup> → 4f<sup>3</sup> [<sup>4</sup>I<sub>J</sub>, <sup>4</sup>F<sub>J</sub>, <sup>4</sup>G<sub>J</sub>] emissions at 178, 225, and 255 nm respectively, and 4f<sup>3</sup> → 4f<sup>3</sup> emission around 875 nm corresponding to the Nd<sup>3+</sup> <sup>4</sup>F<sub>3/2</sub> → <sup>4</sup>I<sub>9/2</sub> transition. The ratio between 5d → 4f and 4f → 4f emissions upon Nd<sup>3+</sup> 5d excitation is controlled to a large extent by the energy gap between the Stokes shifted lowest energy 5d state and the first lower energy 4f<sup>3</sup> state. Only when this gap is small enough [typically <7500 cm<sup>-1</sup> (Ref. 15)], nonradiative feeding of the <sup>2</sup>G<sub>9/2</sub> level of Nd<sup>3+</sup> (around 48.000 cm<sup>-1</sup>) is possible. Under these conditions, a large number of 4f<sup>3</sup> → 4f<sup>3</sup> emission lines in the UV and visible spectral range are observed.<sup>15</sup> Since only very weak 4f<sup>3</sup> → 4f<sup>3</sup> emission lines are observed in NaLaF<sub>4</sub>:Nd<sup>3+</sup>, it must be concluded that 5d → 4f emission is the dominant relaxation route after Nd<sup>3+</sup> 4f → 5d excitation. The observed <sup>4</sup>F<sub>3/2</sub> → <sup>4</sup>I<sub>9/2</sub> emission around 875 nm is the result of radiative feeding of the <sup>4</sup>G<sub>J</sub> (255 nm) and the <sup>4</sup>F<sub>J</sub> (225 nm) states, as indicated in Fig. 3(a).

**B. Down-conversion in NaGdF<sub>4</sub>:2%Nd<sup>3+</sup>**

The emission spectrum of NaGdF<sub>4</sub>:Nd<sup>3+</sup> under Nd<sup>3+</sup> 4f<sup>2</sup>5d<sup>1</sup> excitation at 156 nm is plotted in Fig. 4(a).

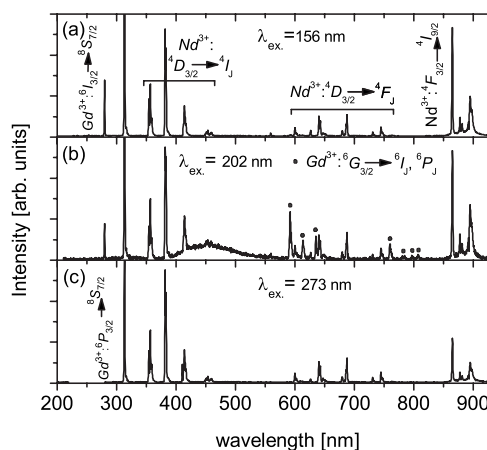


FIG. 4. Emission spectra of NaGdF<sub>4</sub>:2%Nd<sup>3+</sup> recorded at 10 K during (a) Nd<sup>3+</sup> 4f<sup>2</sup>5d<sup>1</sup> → 4f<sup>3</sup> excitation at 156 nm, (b) Gd<sup>3+</sup> <sup>8</sup>S<sub>7/2</sub> → <sup>6</sup>G<sub>J</sub> excitation at 202 nm, and (c) Gd<sup>3+</sup> <sup>8</sup>S<sub>7/2</sub> → <sup>6</sup>I<sub>J</sub> excitation at 273 nm. The three spectra were normalized to the Nd<sup>3+</sup> <sup>4</sup>D<sub>3/2</sub> → <sup>4</sup>I<sub>9/2</sub> transition at 383 nm.

When this emission spectrum is compared with the emission spectrum of NaLaF<sub>4</sub>:Nd<sup>3+</sup>, also excited at 156 nm (Fig. 2), it can be observed that the Nd<sup>3+</sup> 5d → 4f emission is completely quenched in NaGdF<sub>4</sub>:Nd<sup>3+</sup>. Instead, Gd<sup>3+</sup> emission from the <sup>6</sup>P<sub>3/2</sub> and the <sup>6</sup>I<sub>3/2</sub> levels to the <sup>8</sup>S<sub>7/2</sub> ground state is observed at 279 and 313 nm, respectively, as well as emission from the <sup>4</sup>D<sub>3/2</sub> and <sup>4</sup>F<sub>3/2</sub> levels of Nd<sup>3+</sup> [see Fig. 4(a)]. Clearly, energy is transferred completely from the 5d states of Nd<sup>3+</sup> to the 4f levels of Gd<sup>3+</sup>. Figure 4(b) represents the emission spectrum of NaGdF<sub>4</sub>:Nd<sup>3+</sup> under direct Gd<sup>3+</sup> excitation into a <sup>6</sup>G<sub>J</sub> level at 202 nm. At this excitation wavelength, emission from the <sup>6</sup>G<sub>7/2</sub> Gd<sup>3+</sup> level is observed, as indicated by the black dots. Since these emissions were not observed under Nd<sup>3+</sup> 5d excitation, it must be concluded that energy transfer from Nd<sup>3+</sup> to Gd<sup>3+</sup> proceeds to any of the lower energy <sup>6</sup>D<sub>J</sub>, <sup>6</sup>I<sub>J</sub>, and <sup>6</sup>P<sub>J</sub> states of Gd<sup>3+</sup> and not the <sup>6</sup>G<sub>J</sub> states.

This energy transfer route is confirmed by the excitation spectra plotted in Fig. 5 monitoring the Gd<sup>3+</sup> <sup>6</sup>G<sub>7/2</sub> → <sup>6</sup>P<sub>3/2</sub> emission at 592 nm [spectrum (a)] and the Gd<sup>3+</sup> <sup>6</sup>P<sub>3/2</sub> → <sup>8</sup>S<sub>7/2</sub> emission at 313 nm [spectrum (b)]. Spectrum (a) directly proves that <sup>6</sup>G<sub>7/2</sub> emission at 592 nm can only be excited into the <sup>6</sup>G<sub>J</sub> levels themselves but not into the Nd<sup>3+</sup> 5d states. Spectrum (b) confirms that the Gd<sup>3+</sup> <sup>6</sup>P<sub>3/2</sub> → <sup>8</sup>S<sub>7/2</sub> emission at 311 nm is sensitized by the Nd<sup>3+</sup> 5d states.

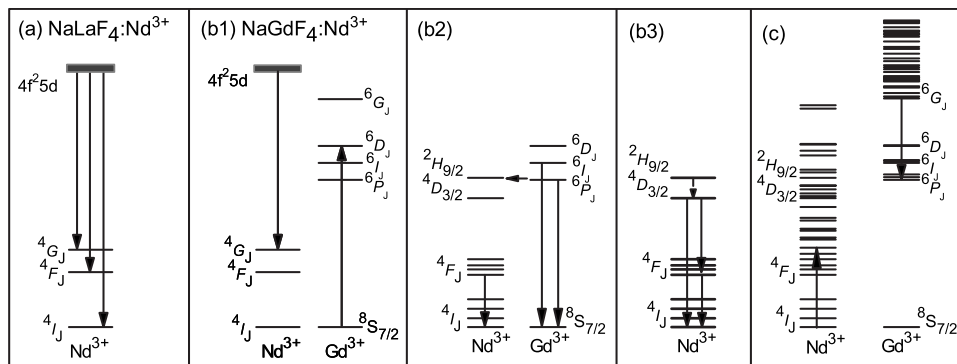


FIG. 3. Schematic energy level diagrams of Nd<sup>3+</sup> and Gd<sup>3+</sup> in (a) NaLaF<sub>4</sub>:2%Nd<sup>3+</sup> and [(b) and (c)] NaGdF<sub>4</sub>:2%Nd<sup>3+</sup> showing the observed radiative and energy transfer relaxation routes after optical excitation of the [(b1)–(b3)] Nd<sup>3+</sup> 5d state and the (c) <sup>6</sup>G<sub>J</sub> states of Gd<sup>3+</sup>. Note that only relevant energy levels are shown.

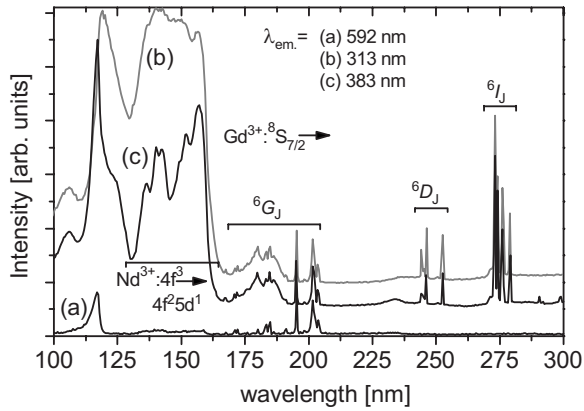


FIG. 5. Excitation spectra of NaGdF<sub>4</sub>:2%Nd<sup>3+</sup> recorded at 10 K monitoring (a) the Gd<sup>3+</sup>  ${}^6G_{7/2} \rightarrow {}^6P_{3/2}$  transition at 592 nm, (b) the Gd<sup>3+</sup>  ${}^6P_{3/2} \rightarrow {}^8S_{7/2}$  transition at 313 nm, and (c) the Nd<sup>3+</sup>  ${}^4D_{3/2} \rightarrow {}^4I_{9/2}$  transition at 383 nm.

The selective energy transfer from the  $5d$  states of Nd<sup>3+</sup> to the lower energy states of Gd<sup>3+</sup> can be explained by a favorable spectral overlap between the lower energy  ${}^6D_J$ ,  ${}^6I_J$ , and  ${}^6P_J$  states of Gd<sup>3+</sup> and the  $4f^25d^1 \rightarrow 4f^3$  emission bands of Nd<sup>3+</sup>. Figures 6(a) and 6(b), representing the Nd<sup>3+</sup>  $5d \rightarrow 4f$  emission and the Gd<sup>3+</sup>  $4f \rightarrow 4f$  excitation spectrum, respectively, indeed confirm a good spectral overlap around 255 nm between Nd<sup>3+</sup>  $4f^25d^1 \rightarrow 4f^3[{}^4G_J]$  emission and Gd<sup>3+</sup>  ${}^8S_{7/2} \rightarrow {}^6D_J$  absorption. Figure 3(b1) shows the identified cross-relaxation process in NaGdF<sub>4</sub>:Nd<sup>3+</sup> that explains the selective energy transfer from Nd<sup>3+</sup> to Gd<sup>3+</sup>.

Jia *et al.*<sup>10</sup> recently studied sensitization of Gd<sup>3+</sup> by Nd<sup>3+</sup> in LiGdF<sub>4</sub>:Nd<sup>3+</sup> and assumed a cross-relaxation process from the  $5d$  states of Nd<sup>3+</sup> to the higher energy  ${}^6G_J$  levels of Gd<sup>3+</sup>. They, however, at the same time, noted that cross relaxation to the lower lying  ${}^6D_J$ ,  ${}^6I_J$ , and  ${}^6P_J$  states of Gd<sup>3+</sup>

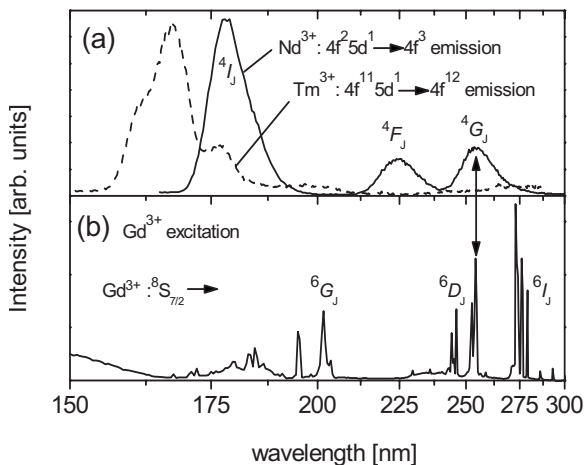


FIG. 6. Spectral energy overlap between the Nd<sup>3+</sup> and Tm<sup>3+</sup>  $5d \rightarrow 4f$  emission and Gd<sup>3+</sup>  $4f \rightarrow 4f$  excitation in NaGdF<sub>4</sub>:2%Nd<sup>3+</sup> and NaGdF<sub>4</sub>:2%Tm<sup>3+</sup>, respectively. (a) Nd<sup>3+</sup> emission spectrum (solid) recorded at 10 K under  $4f^3 \rightarrow 4f^25d$  excitation at 156 nm and the Tm<sup>3+</sup> emission spectrum (dashed) under  $4f^{12} \rightarrow 4f^{11}5d$  excitation at 131 nm. (b) Excitation spectrum recorded at 10 K monitoring the Gd<sup>3+</sup>  ${}^6P_{3/2} \rightarrow {}^8S_{7/2}$  transition at 313 nm.

could not be excluded on the bases of their experimental data. Our data clearly show that in NaGdF<sub>4</sub>:Nd<sup>3+</sup>, the lower energy Gd<sup>3+</sup> levels are sensitized by the  $5d$  states of Nd<sup>3+</sup>. Our conclusion is based on the excitation spectrum monitoring Gd<sup>3+</sup>  ${}^6G_{7/2}$  emission that shows no Nd<sup>3+</sup>  $5d$  excited states [see Fig. 5(a)] and the favorable spectral overlap between the  $5d \rightarrow 4f$  Nd<sup>3+</sup> emission and the Gd<sup>3+</sup>  ${}^8S_{7/2} \rightarrow {}^6D_J$  absorption (Fig. 6). Because no emission from the  ${}^6G_{7/2}$  level of Gd<sup>3+</sup> was observed in LiGdF<sub>4</sub>:Nd<sup>3+</sup>, a simple proof as was given in this work cannot be given. The emission of Nd<sup>3+</sup> in LiGdF<sub>4</sub> is, however, expected to be the same as in LiYF<sub>4</sub>:Nd<sup>3+</sup> (Ref. 10) which, in turn, is the same as in NaGdF<sub>4</sub>:Nd<sup>3+</sup> (compare Ref. 16 and Fig. 6 of this work). Spectral overlap between Nd<sup>3+</sup> emission and Gd<sup>3+</sup> absorption in LiGdF<sub>4</sub>:Nd<sup>3+</sup> will therefore be the same as in NaGdF<sub>4</sub> which suggests that sensitization of the high energy  ${}^6G_J$  levels does not take place in LiGdF<sub>4</sub>:Nd<sup>3+</sup>.

The emission from the  ${}^4D_{3/2}$  state of Nd<sup>3+</sup> [see Fig. 4(a)], which is observed under Nd<sup>3+</sup>  $5d$  excitation, is the result of a partial energy transfer from the  ${}^6P_{3/2}$  level of Gd<sup>3+</sup> to Nd<sup>3+</sup>, as indicated by the vertical arrow in Fig. 3(b2). This transfer is demonstrated by the observation of Nd<sup>3+</sup>  ${}^4D_{3/2}$  emissions under direct Gd<sup>3+</sup>  ${}^8S_{7/2} \rightarrow {}^6I_J$  excitation at 273 nm [see Fig. 4(c)]. In addition, excitation spectrum (c) plotted in Fig. 5, monitoring the Nd<sup>3+</sup>  ${}^4D_{3/2} \rightarrow {}^4I_{9/2}$  emission at 383 nm, clearly reveals the Gd<sup>3+</sup>  ${}^8S_{3/2} \rightarrow {}^6P_J$ ,  ${}^6I_J$ , and  ${}^6G_J$  transitions, which confirms the Gd<sup>3+</sup>  $\rightarrow$  Nd<sup>3+</sup> back transfer.

The above described down-conversion process involving a two step energy transfer process from Nd<sup>3+</sup> to Gd<sup>3+</sup> [step 1, Fig. 3(b1)] and back from Gd<sup>3+</sup> to Nd<sup>3+</sup> [step 2, Fig. 3(b2)] can result in the emission of two IR photons by Nd<sup>3+</sup> ( ${}^4F_{3/2} \rightarrow {}^4I_{9/2}$ ) for each absorbed VUV photon (between 130 and 160 nm). The first cross-relaxation step [Fig. 3(b1)] populates the Nd<sup>3+</sup>  ${}^4F_{3/2}$  state and the Gd<sup>3+</sup>  ${}^6D_{9/2}$  state. Subsequently, the back-transfer step discussed above [Fig. 3(b2)] populates the Nd<sup>3+</sup>  ${}^4D_{3/2}$  levels. Finally, the Nd<sup>3+</sup>  ${}^4F_{3/2}$  state is populated the second time by Nd<sup>3+</sup>  ${}^4D_{3/2} \rightarrow {}^4F_J$  emission [Fig. 3(b3)]. Further experimental evidence for this down-conversion process can be found by comparing the emission spectra plotted in Figs. 4(a) and 4(c) that are both normalized at 383 nm, i.e., the Nd<sup>3+</sup>  ${}^4D_{3/2} \rightarrow {}^4I_{7/2}$  emission line. The enhanced IR emission (around 875 nm) under Nd<sup>3+</sup>  $5d$  excitation [Fig. 4(a)] compared to direct Gd<sup>3+</sup>  ${}^6I_J$  excitation [Fig. 4(c)] is the expected consequence of the down-conversion process described above. Note that, although with poor quantum efficiency, there is a change for emission of three photons for an absorbed VUV photon, i.e., two times  ${}^4F_{3/2} \rightarrow {}^4I_{9/2}$  and one times  ${}^4D_{3/2} \rightarrow {}^4F_J$ .

Finally, it is interesting to note that the emission spectrum obtained under direct Gd<sup>3+</sup>  ${}^6G_J$  excitation at 202 nm, shown in Fig. 4(b), also shows enhanced IR emission compared to  ${}^6I_J$  excitation at 273 nm [Fig. 4(c)]. This can be explained by down-conversion involving a two step energy transfer process from the  ${}^6G_{7/2}$  level of Gd<sup>3+</sup> to the  ${}^4F_{3/2}$  level of Nd<sup>3+</sup> that was described earlier by Jia *et al.*<sup>10</sup> for LiGdF<sub>4</sub>:Nd<sup>3+</sup>. The first step is cross relaxation involving the Gd<sup>3+</sup> [ ${}^6G_{3/2} \rightarrow {}^6P_J$ ] and the Nd<sup>3+</sup> [ ${}^4I_{9/2} \rightarrow {}^4F_J$ ] transitions, as indicated by the vertical arrows in Fig. 3(c), resulting in excitation of the Nd<sup>3+</sup>  ${}^4F_{3/2}$  state and excitation of the Gd<sup>3+</sup>  ${}^6P_{3/2}$  state. The

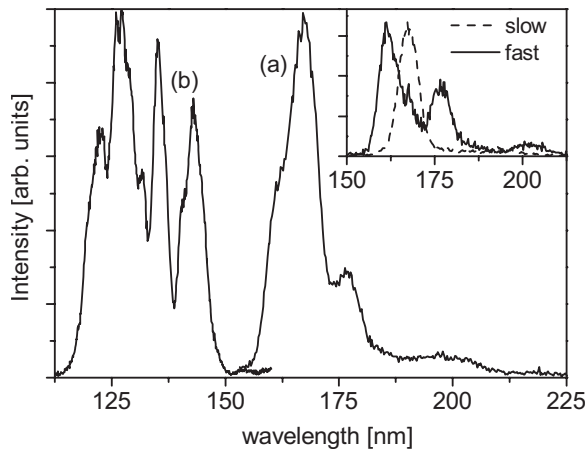


FIG. 7. (a) Excitation spectrum of  $\text{NaLaF}_4:2\% \text{Tm}^{3+}$  recorded at 10 K monitoring the  $\text{Tm}^{3+} 4f^{11}5d^1 \rightarrow 4f^{12}$  emission at 176 nm. (b) Emission spectrum recorded at 10 K excited in the  $4f^{11}5d^1$  states of  $\text{Tm}^{3+}$  at 131 nm. The inset shows time resolved emission spectra recorded after pulsed synchrotron excitation between 2 and 10 ns ("fast") and 80 and 160 ns ("slow").

second step is the previously described back transfer process resulting in excitation of a second  $\text{Nd}^{3+}$  ion into the  ${}^4F_{3/2}$  state [see Figs. 3(b2) and 3(b3)].

From an application point of view, it must be noted that the overall internal quantum efficiency for  $\text{Nd}^{3+} {}^4F_{3/2}$  emission in  $\text{NaGdF}_4:\text{Nd}^{3+}$  under  $\text{Nd}^{3+} 5d$  excitation or direct  $\text{Gd}^{3+}$  excitation is low because the  $\text{Gd}^{3+} {}^6P_{3/2} \rightarrow {}^8S_{7/2}$  and the  $\text{Nd}^{3+} {}^4D_{3/2} \rightarrow {}^4I_J$  emissions contain most of the intensity. In addition, the enhanced  $\text{Nd}^{3+} {}^4F_{3/2}$  emission is located in the IR which is useless for lamp or display applications.

#### C. Vacuum-ultraviolet spectroscopy of $\text{NaLaF}_4:2\% \text{Tm}^{3+}$

Figure 7 shows the emission spectrum [trace (a)] of  $\text{NaLaF}_4:\text{Tm}^{3+}$  recorded during  $\text{Tm}^{3+} 4f \rightarrow 5d$  excitation at 131 nm and the excitation spectrum [trace (b)] monitoring  $\text{Tm}^{3+} 5d \rightarrow 4f$  emission at 176 nm. Unique identification of the  $5d \rightarrow 4f$  emission bands of  $\text{Tm}^{3+}$  is possible by studying

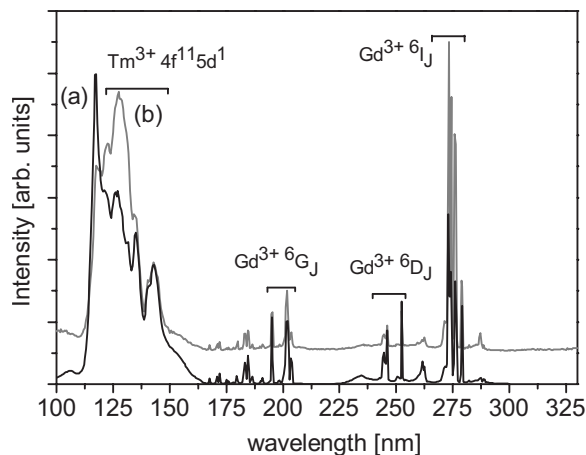


FIG. 8. Excitation spectra of  $\text{NaGdF}_4:2\% \text{Tm}^{3+}$  recorded at 10 K monitoring (a) the  $\text{Gd}^{3+} {}^6P_{3/2} \rightarrow {}^8S_{7/2}$  emission at 313 nm and (b) the  $\text{Tm}^{3+} {}^3P_0 \rightarrow {}^3H_4$  emission at 345 nm.

the time resolved emission spectra plotted in the inset of Fig. 7. The fast component of the emission (solid curve) was recorded between 3 and 10 ns after pulsed synchrotron excitation. The slow component (dashed curve) was recorded between 60 and 180 ns. The emission spectrum is composed of two emission bands at 161.6 and 176.8 nm with a short decay time, which correspond to the spin-allowed  $5d \rightarrow 4f$  transition starting from the high spin  $5d$  state of  $\text{Tm}^{3+}$  (Ref. 16) to the  ${}^3F_4$  and  ${}^3H_6$  states. Another emission band at 167.5 nm with a longer decay time corresponds to the spin-forbidden  $5d \rightarrow 4f$  transition starting from the low spin  $5d$  state of  $\text{Tm}^{3+}$  (Ref. 17) to the  ${}^3H_6$  state. These transitions are indicated in Fig. 10(a). The excitation spectrum monitoring both the spin allowed and spin forbidden  $5d \rightarrow 4f$  transitions around 177 nm, shown in Fig. 7 [trace (b)], consists of  $4f \rightarrow 5d$  excitation bands of  $\text{Tm}^{3+}$  between 120 and 150 nm.

#### D. Down-conversion in $\text{NaGdF}_4:2\% \text{Tm}^{3+}$

Figure 8(a) shows the excitation spectrum of  $\text{NaGdF}_4:\text{Tm}^{3+}$  monitoring  $\text{Gd}^{3+}$  emission at 313 nm. Besides the expected  $\text{Gd}^{3+} 4f^7$  lines, the spectrum contains the same broad band features that were observed in the excitation spectra of  $\text{NaLaF}_4:2\% \text{Tm}^{3+}$  monitoring  $\text{Tm}^{3+} 5d \rightarrow 4f$  emission and are therefore assigned to the  $5d$  states of  $\text{Tm}^{3+}$ . This excitation spectrum therefore proves energy transfer from the  $5d$  states of  $\text{Tm}^{3+}$  to the  $4f$  states of  $\text{Gd}^{3+}$ . The emission spectrum of  $\text{NaGdF}_4:\text{Tm}^{3+}$  recorded under  $\text{Tm}^{3+} 5d$  excitation at 143 nm is plotted in Fig. 9(a). It is dominated by  $\text{Gd}^{3+} {}^6P_{3/2} \rightarrow {}^8S_{7/2}$  emission at 313 nm which confirms efficient energy transfer from  $\text{Tm}^{3+}$  to  $\text{Gd}^{3+}$ .

In Fig. 6, the  $\text{Tm}^{3+} 5d \rightarrow 4f$  emission spectrum is compared with the  $\text{Gd}^{3+}$  excitation spectrum. It shows that the  $5d \rightarrow 4f$  emission only has spectral overlap with the  ${}^6G_J$  states of  $\text{Gd}^{3+}$ . Contrary to the situation for  $\text{NaGdF}_4:\text{Nd}^{3+}$ , there is no  $5d \rightarrow 4f$  emission overlapping with the lower energy  ${}^6D_J$ ,  ${}^6I_J$ , and  ${}^6P_J$  states of  $\text{Gd}^{3+}$ . This strongly suggests that energy is transferred from the  $5d$  states of  $\text{Tm}^{3+}$  to the  ${}^6G_J$  state of  $\text{Gd}^{3+}$ , as indicated by the curved arrows in

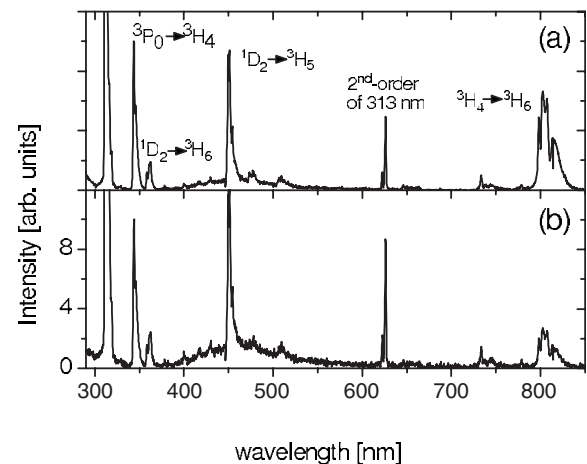


FIG. 9. Emission spectra of  $\text{NaGdF}_4:2\% \text{Tm}^{3+}$  recorded at 10 K during (a)  $\text{Tm}^{3+} 4f^{12} \rightarrow 4f^{11}5d^1$  excitation at 143 nm and (b)  $\text{Gd}^{3+} {}^8S_{7/2} \rightarrow {}^6D_J$  excitation at 252 nm. The two spectra were normalized at the  ${}^3P_0 \rightarrow {}^3H_4$  transition.

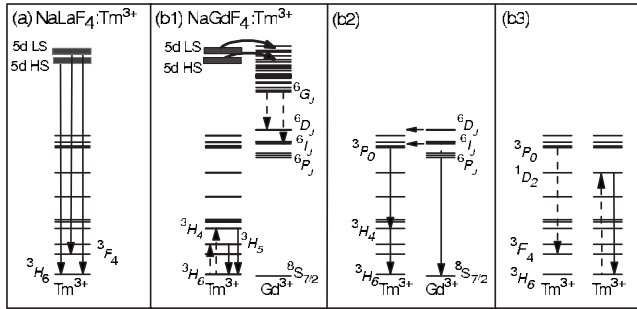


FIG. 10. Schematic energy level diagram of  $\text{Tm}^{3+}$  in  $\text{NaLaF}_4$  and the observed spin-allowed and spin-forbidden  $4f^{11}5d^1 \rightarrow 4f^{12}$  transitions. (b) Energy level diagram of  $\text{Tm}^{3+}$  and  $\text{Gd}^{3+}$  in  $\text{NaGdF}_4:2\% \text{Tm}^{3+}$  showing the observed radiative and energy transfer relaxation routes after optical excitation of (b1)–(b3) the  $5d$  state of  $\text{Tm}^{3+}$ . Note that for clarity, not all energy levels have been drawn.

Fig. 10(b1). The same type of transfer was observed in  $\text{LiGdF}_4:\text{Tm}^{3+}$  by Peijzel *et al.*<sup>9</sup>

Figure 9(a) shows no evidence of emission from  ${}^6G_{3/2}$  state of  $\text{Gd}^{3+}$ . Instead, it shows strong  $\text{Gd}^{3+} {}^6P_{3/2}$  emission at 313 nm and emission from the  $\text{Tm}^{3+} {}^3H_4$  state around 800 nm. Since there is no direct transfer route from the  $5d$  states of  $\text{Tm}^{3+}$  to the  $\text{Gd}^{3+} {}^6P_{3/2}$  state, and no  $\text{Gd}^{3+} {}^6G_{3/2}$  emission is observed, there must be an efficient cross relaxation between  $\text{Tm}^{3+}$  and  $\text{Gd}^{3+}$ . The most likely cross-relaxation route that was also adopted by Peijzel *et al.* for  $\text{LiGdF}_4:\text{Tm}^{3+}$  is indicated by the dashed arrows in Fig. 10(b1). Cross relaxation involves the transitions  ${}^6G_{3/2} \rightarrow {}^6I_J$ ,  ${}^6D_J$  on  $\text{Gd}^{3+}$  and  ${}^3H_4 \rightarrow {}^3H_6$ ,  ${}^3H_5$  on  $\text{Tm}^{3+}$  and thus explains not only the emission from the  ${}^6P_{3/2}$  state of  $\text{Gd}^{3+}$  (after nonradiative relaxation from the  ${}^6I_J$ ,  ${}^6D_J$  states) upon  $\text{Tm}^{3+} 5d$  excitation but also the emission from the  ${}^3H_4$  state of  $\text{Tm}^{3+}$ .

Figure 8(b) shows the excitation spectrum of  $\text{NaGdF}_4:2\% \text{Tm}^{3+}$  monitoring the  $\text{Tm}^{3+} {}^3P_0 \rightarrow {}^3H_4$  emission at 345 nm. The spectrum shows that  $\text{Tm}^{3+} {}^3P_0$  emission can be excited into the  ${}^6G_J$ ,  ${}^6D_J$ , and  ${}^6I_J$  states of  $\text{Gd}^{3+}$  but not in the  ${}^6P_J$  states. This is explained by the energy level diagrams of  $\text{Gd}^{3+}$  and  $\text{Tm}^{3+}$  [see Fig. 10(b2)], which show no possibility for energy transfer from  $\text{Gd}^{3+} {}^6P_J$  state to the  $\text{Tm}^{3+} {}^3P_0$  state because it is located at a too low energy. This explains the high intensity of the  $\text{Gd}^{3+} {}^6P_{3/2}$  emission. The observed  ${}^3P_0$  emission must therefore be the result of transfer from the  ${}^6I_{3/2}$  and  ${}^6D_{3/2}$  states of  $\text{Gd}^{3+}$ , as indicated by the horizontal arrows in Fig. 10(b2).

The emission from the  ${}^1D_2$  state observed under  $\text{Tm}^{3+} 5d$  excitation cannot be explained by nonradiative  $4f \rightarrow 4f$  relaxation from the  ${}^3P_0$  state to the  ${}^1D_2$  state given the large energy gap and the low phonon energy characteristic of the  $\text{NaGdF}_4$  host. A radiative feeding from the excited  $\text{Tm}^{3+} 5d$  state can also be excluded since no corresponding emission is observed.  ${}^1D_2$  emission is therefore explained by cross relaxation between nearest neighbor  $\text{Tm}^{3+}$  ions, as indicated by the dashed arrows in Fig. 10(b3).

In Fig. 9(a), the  $\text{Tm}^{3+} 4f^{12} \rightarrow 4f^{11}5d^1$  transition is excited at 143 nm, whereas the  $\text{Gd}^{3+} {}^8S_{7/2} \rightarrow {}^6D_J$  transition is excited at 252 nm in Fig. 9(b). The two spectra, normalized at the maximum of the  ${}^3P_0$  emission line at 345 nm, are largely the

same except for an enhanced  $\text{Tm}^{3+} {}^3H_4 \rightarrow {}^3H_6$  emission under  $\text{Tm}^{3+} 5d$  excitation. This enhanced  ${}^3H_4$  emission can be explained by the two successive cross-relaxation steps from  $\text{Gd}^{3+}$  to the  ${}^3H_4$  state of  $\text{Tm}^{3+}$ , which were described above. The first step is cross relaxation between  $\text{Gd}^{3+}$  and  $\text{Tm}^{3+}$  involving the transitions  ${}^6G_{7/2} \rightarrow {}^6I_J$  on  $\text{Gd}^{3+}$  and  ${}^3H_6 \rightarrow {}^3H_4$  excitation of  $\text{Tm}^{3+}$  [see Fig. 10(b1)]. This cross relaxation results in the first excited  $\text{Tm}^{3+}$  ion in the  ${}^3H_4$  state. In the second step, energy is transferred from the  ${}^6D_{3/2}$  and  ${}^6I_{3/2}$  states of  $\text{Gd}^{3+}$  to the  ${}^3P_0$  state of  $\text{Tm}^{3+}$ , as indicated by the horizontal arrow in Fig. 10(b2). This transfer process can result in excitation of a second  $\text{Tm}^{3+}$  ion in the  ${}^3H_4$  state after  ${}^3P_0 \rightarrow {}^3H_4$  emission, as indicated in Fig. 10(b2).

The weak  $\text{Tm}^{3+} {}^3P_0$ ,  ${}^1D_2$ , and  ${}^3H_4$  emissions, as shown in Fig. 8(b) (the latter emission caused by radiative feeding from the  ${}^3P_0$  state), compared to the  $\text{Gd}^{3+} {}^6P_{3/2}$  emission are caused by a far more efficient nonradiative relaxation on  $\text{Gd}^{3+}$  from the  ${}^6I_{3/2}$  and  ${}^6D_{3/2}$  states to the  ${}^6P_{3/2}$  state compared to energy transfer from  $\text{Gd}^{3+}$  to the  ${}^3P_0$  state of  $\text{Tm}^{3+}$ . It must, however, be noted that the cross-relaxation step from the  ${}^6G_{7/2}$  step to the  ${}^3H_4$  and  ${}^3H_5$  states [Fig. 10(b1)] predicts an equally intense  $\text{Gd}^{3+} {}^6P_{3/2}$  emission compared to  $\text{Tm}^{3+} {}^3H_4$  and  ${}^3H_5$  emissions. Since only weak  ${}^3H_4$  emission is observed, it must be concluded that cross relaxation mainly involves the  ${}^3H_5$  state that has emission around 1250 nm which is outside the sensitive area of our CCD detector.

#### IV. CONCLUSIONS

VUV to IR luminescence excitation and emission measurements have revealed in detail how energy relaxes back to the ground state via complex energy transfer and emission scenarios after VUV excitation into the  $5d$  states of  $\text{Nd}^{3+}$  and  $\text{Tm}^{3+}$  in  $\text{NaGdF}_4$ . In both systems, quantum splitting is observed that can result in the emission of two IR photons for each absorbed VUV photon.

$\text{Nd}^{3+} 4f^2 5d^1 \rightarrow 4f^3$  emission in  $\text{NaLaF}_4:2\% \text{Nd}^{3+}$  is quenched in  $\text{NaGdF}_4$  by an identified cross-relaxation process involving the transitions  $4f^2 5d^1 \rightarrow 4f^3$  ( ${}^4G_J$ ) on  $\text{Nd}^{3+}$  and  ${}^8S_{7/2} \rightarrow {}^6D_J$  on  $\text{Gd}^{3+}$ . This results in  $\text{Nd}^{3+}$  emission from the  ${}^4F_{3/2}$  state in the IR after nonradiative relaxation from the  ${}^4G_J$  state. A second photon from the  ${}^4F_{3/2}$  state of  $\text{Nd}^{3+}$  can be emitted after  $\text{Gd}^{3+} ({}^6P_{3/2}) \rightarrow \text{Nd}^{3+} ({}^2H_{9/2})$  energy transfer followed by  $\text{Nd}^{3+} {}^2H_{9/2} \rightarrow {}^4D_{3/2}$  nonradiative relaxation and  $\text{Nd}^{3+} {}^4D_{3/2} \rightarrow {}^4F_{3/2}$  emission. Direct excitation of the  $\text{Gd}^{3+} {}^6G_{7/2}$  state in  $\text{NaGdF}_4:2\% \text{Nd}^{3+}$  results in quantum splitting through down-conversion as described recently by Jia *et al.*<sup>10</sup> in  $\text{LiGdF}_4:\text{Nd}^{3+}$ .

$\text{Tm}^{3+} 4f^{11} 5d^1 \rightarrow 4f^{12}$  emission in  $\text{NaLaF}_4:\text{Tm}^{3+}$  is quenched in  $\text{NaGdF}_4$  by cross relaxation involving the spin-allowed and spin-forbidden  $4f^{11} 5d^1 \rightarrow 4f^{12}$  ( ${}^3H_6$ ,  ${}^3F_4$ ) transitions on  $\text{Tm}^{3+}$  and the  ${}^8S_{7/2} \rightarrow {}^6G_J$  transitions on  $\text{Gd}^{3+}$ . This cross-relaxation step results in weak IR  $\text{Tm}^{3+}$  emission from the  ${}^3H_4$  and  ${}^3H_5$  states and strong  $\text{Gd}^{3+} {}^3P_{3/2}$  emission. After cross relaxation, a small fraction of energy is transferred from the  ${}^6D_J$  and  ${}^6I_J$  states of  $\text{Gd}^{3+}$  to the  ${}^3P_0$  state of  $\text{Tm}^{3+}$  which is followed by  $\text{Tm}^{3+} {}^3P_0 \rightarrow {}^3H_4$  emission and successive  ${}^3H_4 \rightarrow {}^3H_6$  emission. In this case, three photons are emitted for one absorbed VUV photon.

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